

Hydraulic and Geometrical Relationships of LAY-FLAT

IRRIGATION TUBING

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Hydraulic and Geometrical Relationships of LAY-FLAT IRRIGATION TUBING¹

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Lay-flat tubing lies flat when empty like a deflated inner-tube section. The tubing is usually made from such materials as butyl rubber or plastic in which a supporting fabric is often built into the walls to impart additional strength.

It is often feasible in irrigation practice to replace farm ditches and laterals with lay-flat tubing, particularly in areas where seepage and erosion are problems. In addition, lay-flat tubing may be used for water distribution, as a temporary water conveyance, or as a conveyance where a ditch would be undesirable or impractical. Use of lay-flat tubing for irrigation is a relatively recent development. Consequently, information is not available to guide fabrication or to design properly a water distribution system hydraulically where it is used. The investigation was undertaken to obtain information that would be useful in the hydraulic design of a water distribution system where lay-flat tubing is used. The principal objectives were (1) to obtain data from static head measurements from which the tube pressure-area-shape relationships could be determined; and (2) to determine a shape factor that would express the effect of cross-sectional shape upon the frictional head loss and allow conventional pipe design formulas to be modified and used for lay-flat tubing.

¹The experimental study summarizes a master's thesis by Allan S. Humphreys, which is on file in the Engineering Library, Utah State University, Logan, and entitled, "An Experimental Study of the Pressure-Area-Shape Relationships of Lay-Flat Tubing and Their Effect Upon the Hydraulic Friction Factor f ." The testing and laboratory phase of the study was undertaken cooperatively with the U.S. Department of Agriculture and the Utah Agricultural Experiment Station.

²The authors express appreciation to the Union Carbide Plastics Co., Division of Union Carbide Corp., for financial support given to the investigation and for the experimental tubing used in both the static and flow tests; to Bono Products, Inc., for butyl rubber tubing furnished for the static tests; to Vaughn E. Hansen, director, Utah Engineering Experiment Station, for his helpful suggestions and technical assistance; and to Richard Miles for assistance in the collection of data.

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HEAD LOSS IN FLOW CONDUITS

PIPE

Because of the similarity between lay-flat tubing and rigid pipe when used as closed conduits for fluid flow, the hydraulic design of tubing should be similar to that of a pipe.

Head loss for flow through a pipe is often expressed in the form³

$$h_f = K \frac{LV^2}{D^m} \quad (1)$$

FIGURE 1.—Definition sketch showing lay-flat tubing geometry.

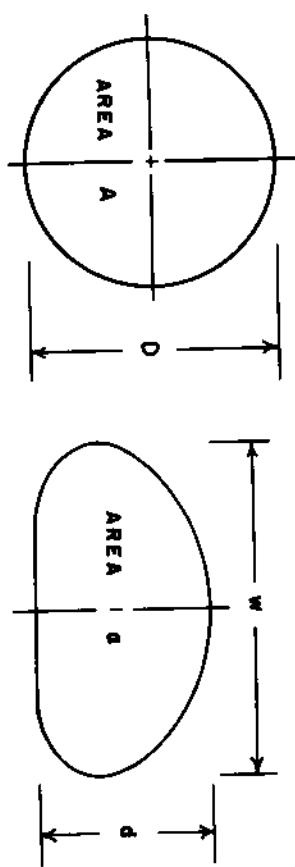
PROBLEM

The shape or degree of roundness and the cross-sectional area of a tube are dependent primarily upon the fluid pressure inside (fig. 1). Above a certain pressure, the tubing approaches a circular cross section. When circular, the tube may be designed hydraulically by conventional pipe design methods. When the pressure inside the tube is reduced, the cross-sectional area becomes smaller and approaches an oval-to-rectangular shape. This change in shape and area results in a nonuniform velocity distribution in which the velocity pattern is different in the vertical direction from that in the horizontal. For a given flow, this change in tube cross section is accompanied by a corresponding change in the mean fluid velocity. The head loss, therefore, is affected, since it is a function of both the velocity distribution and the mean velocity.

Most friction loss in a pipe or tube is dissipated near the boundary because of boundary drag. When the area and degree of roundness for a given tube are decreased, the boundary area becomes larger in proportion to the cross-sectional area. The energy loss, therefore, is affected by any change in tubing geometry that affects the ratio of the cross-sectional area to the perimeter or hydraulic radius.

Not all tubing is hydraulically smooth. Thin tubing constructed with a supporting fabric in its wall may be hydraulically rough. The relative roughness of this tubing is affected by a change in tube shape. Relative roughness is defined as the ratio of the height of the boundary roughness projections⁴ to the depth of flow midway between boundaries. It is usually expressed in terms of the pipe diameter and the plate spacing for pipe and parallel-boundary flow. A decrease in the degree of tubing roundness results in a greater relative roughness value for a given tube, because the effective depth of flow between boundaries is decreased. Since the friction coefficient is related to both the relative roughness and velocity distribution, any shape change that affects either of these parameters will affect the head loss.

In most cases, the pressure along the length of the tube changes because of friction loss and elevation changes. As a result, the tube geometry and, hence, the fluid velocity are constantly changing from one section to another along the length of the tube. The flow, in this case, is nonuniform and the head loss due to friction in a given length of tubing is difficult to determine.



in which the value of n for laminar flow is unity, whereas for turbulent flow it ranges from 1.7 for smooth pipe to 2.0 for rough pipe.⁴ The value of m for laminar flow is 2.0, whereas for turbulent flow its value ranges from 1.0 to approximately 1.3.

Dimensional analysis yields the following expression for pipe friction loss:

$$h_f = 2K R^{n-2} \frac{L}{D} \frac{V^2}{2g} \quad (2)$$

or

$$\frac{1}{\sqrt{f}} = 2 \log_{10} R \sqrt{f} - 0.8. \quad (4)$$

The companion equation for the rough-pipe coefficient is

$$\frac{1}{\sqrt{f}} = 2 \log_{10} \frac{r_o}{k} + 1.74. \quad (5)$$

These equations are valid for the limiting boundary conditions of smooth and rough flow only. The coefficient for flow in the transition region between smooth and rough boundaries for commercial pipe is represented by the semiempirical Colebrook-White equation

$$\frac{1}{\sqrt{f}} = 1.74 - 2 \log_{10} \left[\frac{k}{r_o} + \frac{18.7}{R \sqrt{f}} \right] \quad (6)$$

³RUSSEL, G. E. HYDRAULICS. Ed. 5. Pp. 181-183, illus. New York. 1947.

⁴Symbols and definitions of terms used in this publication are given on p. 38. ROUSE, HUNTER. ELEMENTARY MECHANICS OF FLUIDS. 376 pp., illus. New York and London. 1946.

PARALLEL BOUNDARIES

The flow regime for uniform flow through lay-flat tubing ranges from that for rigid pipe to that for flow through parallel-boundary conduits. Rigid pipe and parallel boundaries represent the extreme conduit shapes. Therefore, expressions for the friction coefficients for flow through parallel boundaries, corresponding to those for pipe flow, are presented. The Karmann-Prandtl equation for the resistance factor for smooth parallel boundaries of infinite extent is

$$\frac{1}{\sqrt{f}} = 2.03 \log_{10} R \sqrt{f} - 0.47. \quad (7)$$

The equation for the parallel rough-boundary coefficient is

$$\frac{1}{\sqrt{f}} = 2.03 \log_{10} \frac{B/2}{k} + 2.11. \quad (8)$$

Because of insufficient data, the constants in equations 7 and 8 have not been adjusted to provide agreement with experimental measurements.

The equations for pipe and parallel-boundary flow are identical except for the integration constant. The factor 2.03 was adjusted to 2 in the pipe equations, to provide better agreement with experimental measurements. Since this factor appears in the expressions for both cross sections, the effect of conduit shape upon the friction factor must be represented by the integration constant for each type of flow.

The Darcy-Weisbach equation for parallel-boundary flow is

$$h_f = f \frac{L}{2B} \frac{V^2}{2g}. \quad (9)$$

The diameter in equation 3 and twice the boundary spacing in equation 9 are each equal to four times the hydraulic radius for their respective cross-sectional shapes. Therefore, if the diameter and twice the boundary spacing are replaced by four times the hydraulic radius, the Darcy-Weisbach equation becomes

$$h_f = f \frac{L}{4R} \frac{V^2}{2g} \quad (10)$$

for both pipe and parallel-boundary flow.

LAY-FLAT TUBING

Keulegan⁶ proposed equations for the friction coefficient for open channels of various cross sections in which the channel shape was

represented by a shape factor term in the expression. To the authors' knowledge, however, no equations have been developed for closed conduit flow covering the entire shape range between round and rectangular.

Since the general head-loss equation, equation 10, is the same for both pipe and parallel-boundary flow and since the expressions for f are the same at each end of the flow regime except for the constants embodying the shape effect, the friction loss through tubing may also be represented by this equation, inasmuch as lay-flat tubing represents a conduit that varies in shape from round to rectangular. It is necessary, however, to modify the friction coefficient to include the effects of shape change. When equation 10 is used for lay-flat tubing, f may be considered as consisting of two parts: (1) f' , the friction coefficient for an equivalent flow through a pipe of the same diameter, and (2) a shape factor β , which corrects f' for the effects of tube shape. In other words

$$f = \beta f'. \quad (11)$$

Thus, the frictional head loss for uniform flow through lay-flat tubing may be represented by

$$h_f = \beta f' \frac{L}{4R} \frac{V^2}{2g} \quad (12)$$

in which β and R are the shape factor and hydraulic radius, respectively, for a given cross-sectional shape. The friction coefficient f' may be obtained from a conventional pipe resistance diagram of f/f' versus Reynolds number. The shape factor β represents the ratio f/f' and is evaluated empirically from flow test data obtained in this study.

HYDROSTATIC TESTS

As pointed out by Hansen,⁷ a study of the hydraulic properties of lay-flat tubing must be preceded by a study of the tube cross-sectional shape and area. Since the head loss and flow capacity of a conduit are a function of the conduit geometry, it is necessary, in studying tubing hydraulics, that its geometry at all pressure heads be known. It is also necessary to know the pressure head and velocity at a given location.

It would be difficult and generally impractical, because of the nature of the material, to install instruments to measure the flow velocity. If the cross-sectional area were known, the mean flow velocity could easily be determined from the continuity equation $Q = aV$ at any point along the tube. As further indicated by Hansen, it may not be practical in some cases to attach pressure gages or taps to determine the piezometric pressure head at a location. The tubing geometry might be utilized for these purposes if data were available that related the tube geometry to the pressure head and cross-sectional area. These relationships were determined from hydrostatic tests made in the laboratory as herein described. The data are plotted in

⁶ KEULEGAN, G. H. LAWS OF TURBULENT FLOW IN OPEN CHANNELS. [U.S. Natl. Bur. Standards Jour. Res. 21: 707-741. (Res. Paper 1151.) 1938.]

⁷ HANSEN, V. E. FLEXIBLE PIPE FOR IRRIGATION WATER UNDER LOW PRESSURE. Agr. Engin. 35(1): 32-33, 39. 1954.

dimensionless ratios and are, therefore, applicable to tubes of different diameters.

EXPERIMENTAL TESTS

Tubing Material Tested

Hydrostatic tests were made on tubes of different materials and sizes (table 1) in which the tube cross section was traced at different hydrostatic pressures. Two types of tubing were used: (1) a thin-walled vinyl chloride plastic and (2) a comparatively thick-walled butyl rubber tube. A 3-inch-diameter vinyl chloride tube was supported by rayon, whereas the rest of the vinyl chloride plastic tubes were supported by nylon. The butyl rubber tubes were also supported with nylon. The vinyl chloride tubes having a wall thickness of 0.01 inch were very flexible. As a result, the resistance to bending offered by the walls of these tubes would be very slight and, therefore, have little effect upon the area relationships. The butyl rubber tubes, however, with a wall thickness of 0.065 inch would offer a greater resistance to bending and were tested to determine the influence of tubing wall thickness upon the shape characteristics.

TABLE 1.—*Description of lay-flat tubing used in hydrostatic tests*

Tubing material	Nominal diameter	Actual diameter	Tubing wall thickness	Supporting structure
Polyvinyl chloride plastic.	Inches 3	Inches 2.90	inch 0.017	Rayon (23 X 23 twined per inch).
	4	4.17	.010	Nylon.
	6	5.60	.010	Do.
Butyl rubber.	8	8.00	.014	Nylon (52 X 30 leno weave).
	12	11.70	.010	Nylon.
	12	13.92	.065	Do.
	4	5.95	.065	Do.
	6	8.40	.065	Do.
	8	11.60	.065	Do.
	12			

Testing Procedure

The tube in which the cross section was to be measured was supported on a sheet of plywood leveled in each direction. Fittings were attached to the tube in such a manner that water could be admitted to the tube and drained from it. A manometer lead was also attached to the tube and connected to a manometer from which the piezometric pressure head was measured. The tube length varied with diameter, but it was at least 10 diameters long. This allowed a minimum of 5 diameters between the end and the section where the tube cross section was traced. The effect of round end fittings upon the cross-sectional shape was thus eliminated.

A special pantograph was constructed and used to trace the cross-sectional shape of the tubes at different hydrostatic pressures. With

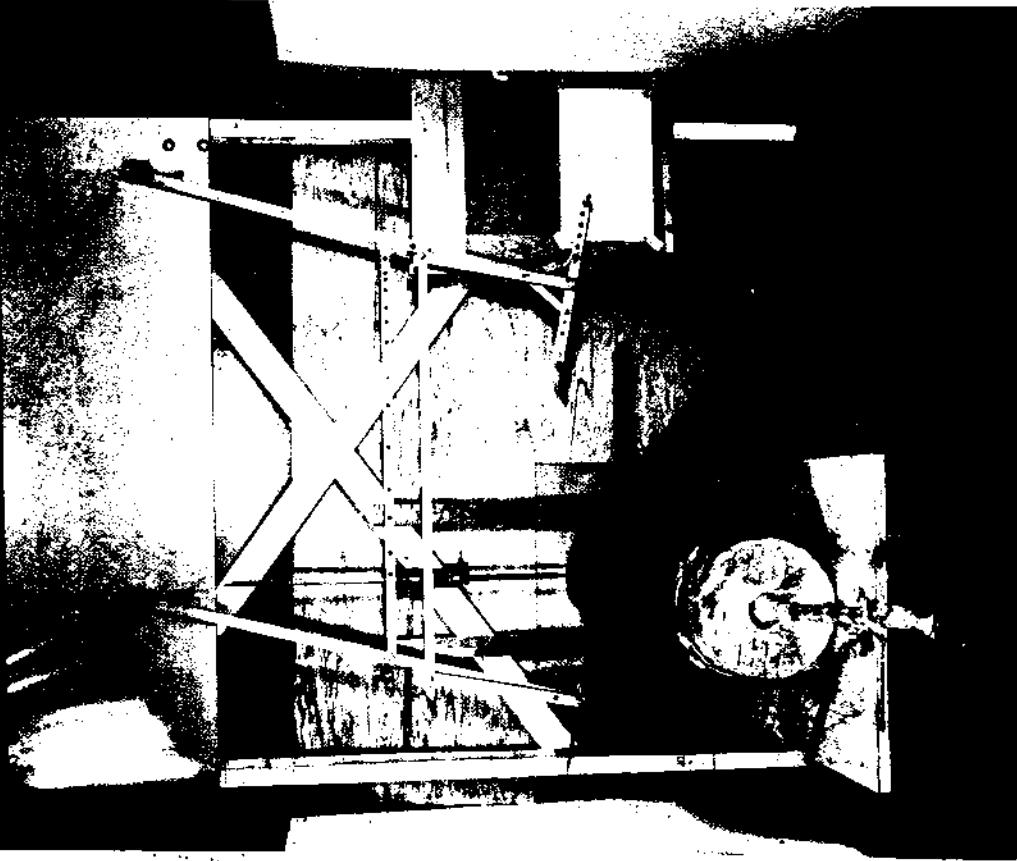


FIGURE 2.—Pantograph and experimental setup for tracing the cross section of lay-flat tubing.

this device, the cross sectional shape of the tube was traced on a sheet of paper as a pointer was moved around the outside perimeter of the tube. The pantograph and the experimental installation are shown in figure 2.

Tracings were made at various hydrostatic pressure heads so that a plot of pressure versus cross-sectional area resulted in a well-defined

curve over the entire shape range from lay-flat to round. Duplicate tracings were made of the tube cross-sectional area at each pressure head.

The vertical-height dimension of the tube was measured for each tracing by a point gage mounted on the pantograph support stand directly over the center of the tube. The horizontal-width dimension of the larger tubes was determined by measuring the distance between two T-squares set adjacent to the tube on each side. The width of the smaller tubes was measured with calipers. Since the tube perimeter changed with the pressure, it was also measured.

Similar measurements were also made to determine the height, width, and area relations of tubing filled with fluids of different specific weights. Tracings were made on an 8-inch vinyl tube with each of the following fluids:

- (1) brine, specific weight = 72.5 lb./cu. ft.
- (2) tapwater, specific weight = 62.5 lb./cu. ft.
- (3) kerosene, specific weight = 50.3 lb./cu. ft.

DATA ANALYSIS AND PRESENTATION

The areas of the cross-sectional tracings were determined with a planimeter. A pressure head vs. area curve was drawn from the average area of the duplicate tracings for each tube. The data, in general, defined a smooth curve, and values for determining the tube cross-sectional area at various hydrostatic pressure heads were taken from these curves. A typical curve for a given tube is shown in figure 3. Since the perimeter changed because of elongation of the tubing material when under pressure, it was necessary to measure the perimeter of the tube section for each tracing. The measured perimeter was then plotted versus the static head for each tube, as shown in figure 3. The perimetric value used to calculate the full-round tube area A was taken from this curve. The ratio, a/A , of the tube area at less than full round to that at full round was computed from the area a , taken from the head-area curves, and the calculated value of A .

The individual pressure head-area curves, such as the one shown in figure 3, were generalized for tubes of all diameters when the data were plotted in dimensionless ratios. This was accomplished by plotting the pressure head as H/D and the area as the ratio a/A . In a similar manner, data representing all of the tube geometrical relations were plotted in dimensionless ratios and, therefore, are applicable to tubes of different sizes. The tube height, width, area, height-width ratio, and hydrostatic head were represented by the ratios d/D , w/D , a/A , d/w , and H/D , respectively, where D is the diameter of a tube when full round. Symbols representing tubing geometry are shown in figure 1.

Vinyl Chloride Plastic Tubes

The parameters H/D , d/w , and d/D for the vinyl chloride plastic tubes are simultaneously related to the tube area in figure 4. The area-tube width relation for this tubing is represented by the curve shown in figure 5. When related to tube width, the area of the

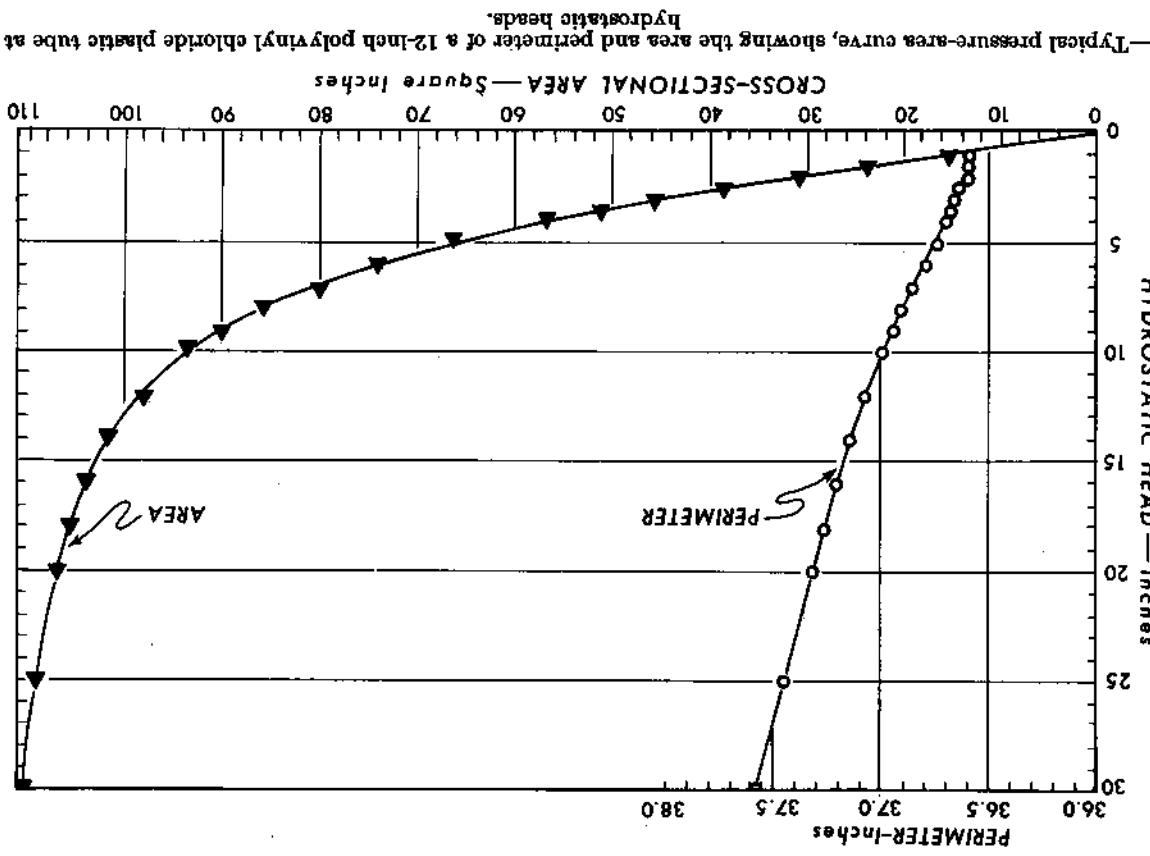


FIGURE 3.—Typical pressure-area curve, showing the area and perimeter of a 12-inch polyvinyl chloride plastic tube at different hydrostatic heads.

FIGURE 4.—The area ratio of lay-flat polyvinyl chloride plastic tubing related to the tube height, hydrostatic head, and tube height-width ratio.

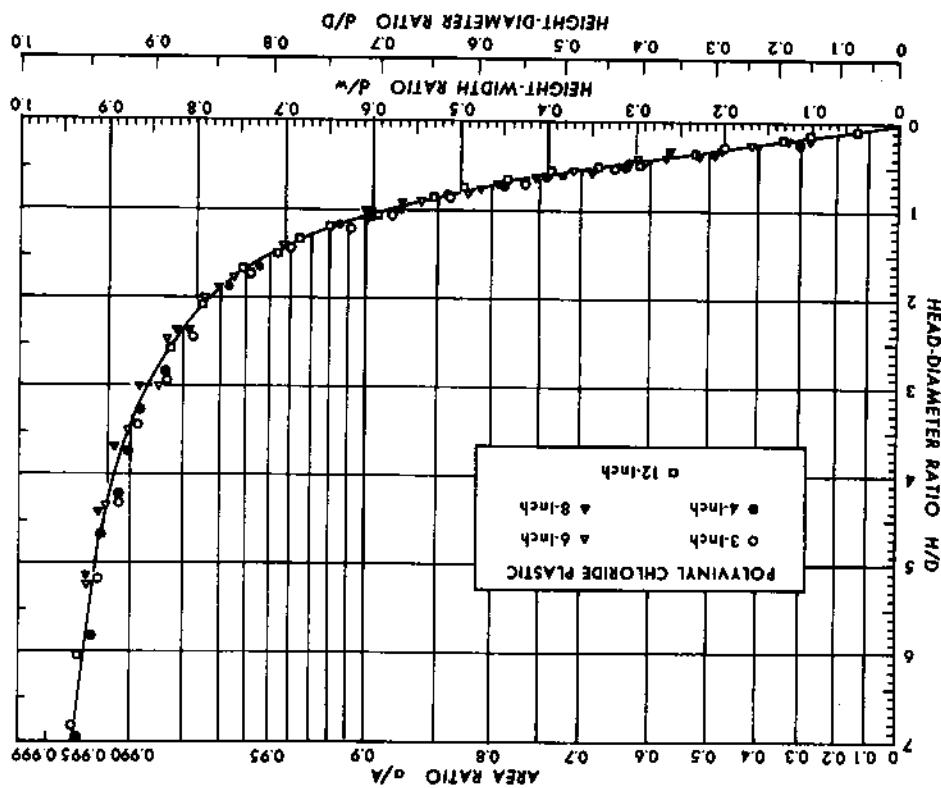
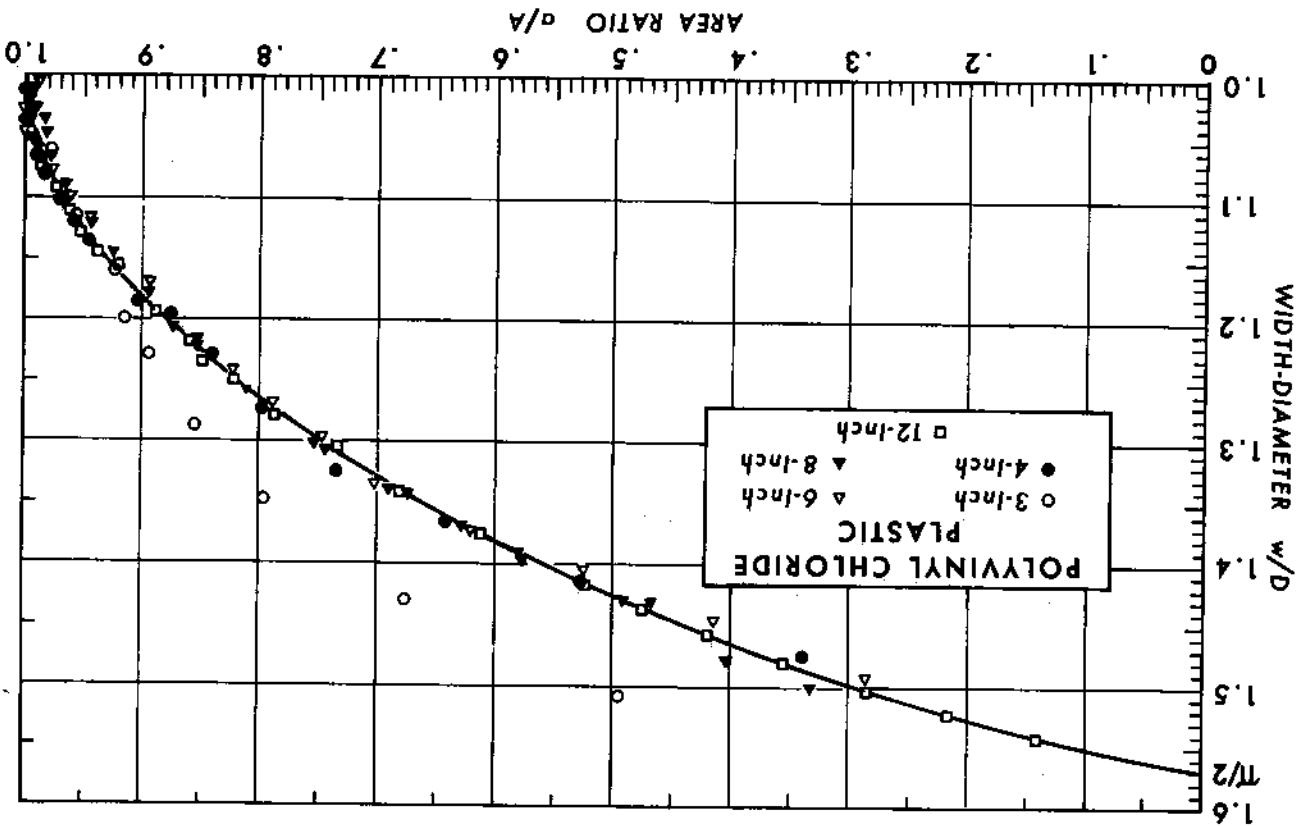


FIGURE 5.—Tube width related to the area of lay-flat polyvinyl chloride plastic tubing.



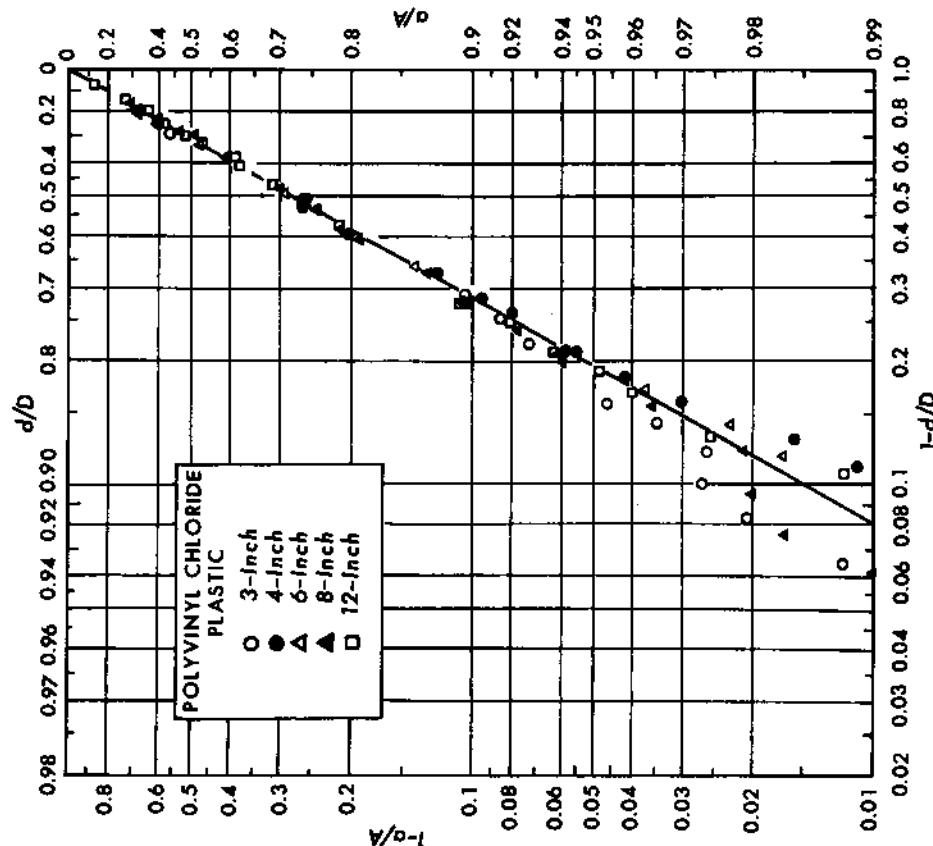


FIGURE 6.—Relation of tube height to the area on logarithmic plot for lay-flat polyvinyl chloride plastic tubing.

3-inch tube did not follow the same curve as the other tubes, because of its greater wall rigidity. The material from which this particular tube was fabricated was less flexible than that for the other vinyl tubes. Because of the flexibility and slight resistance to bending offered by the walls of the vinyl chloride plastic tubing 4 inches and larger in diameter, the data for these tubes represent most accurately the true pressure head and shape-area relationships.

Although these relations are given for water, they are also applicable for other fluids, provided the pressure head is expressed in terms of the particular fluid used. The effect of fluids other than water on tubing geometry is discussed later (p. 18).

An empirical mathematical expression was determined for the area-tube height relationship. This was plotted as $(1-a/A)$ vs. $(1-d/D)$, which on logarithmic coordinate paper yielded a straight line (fig. 6). Although the area-tube height relationship is parabolic,

a log-log plot of a/A vs. d/D directly did not yield a straight line, because the vertex of the parabola was not at the origin. It was necessary, therefore, to adjust the data by subtracting the area-tube height ratios from 1 to obtain a straight line relationship on the log-log plot. The general form of the equation for the line is $y=ax^b$, in which $a=1$ and $b=1.84$. The relationship, therefore, is

$$(1-a/A) = (1-d/D)^{1.84} \quad (13)$$

$$a/A = 1 - (1-d/D)^{1.84}. \quad (14)$$

The term $(1-d/D)^{1.84}$ was expanded by the binomial theorem

$$(a \pm b)^n = a^n \pm na^{n-1}b + \frac{n(n-1)}{2!}a^{n-2}b^2 \pm \frac{n(n-1)(n-2)}{3!}a^{n-3}b^3 + \dots \quad (15)$$

in which

$$(a \pm b)^n = (1-d/D)^{1.84}. \quad (16)$$

The term expanded became

$$(1-d/D)^{1.84} = 1 - 1.84(d/D) + 0.773(d/D)^2 + 0.0412(d/D)^3 + 0.0112(d/D)^4 + 0.0052(d/D)^5 + \dots \quad (17)$$

This expression substituted in equation 14 yielded

$$\begin{aligned} a/A &= 1.84(d/D) - 0.773(d/D)^2 - 0.0412(d/D)^3 \\ &\quad - 0.0112(d/D)^4 - 0.0052(d/D)^5 - \dots \end{aligned} \quad (18)$$

An empirical expression was also determined for the area-tube width relationship in which the parameters $(1-a/A)$ and $(w/D-1)$ on a log-log plot yielded approximately a straight line (fig. 7). The straight line does not fit the data at the end of the curve where the end point value for the extreme lay-flat shape limit is $\pi/2$. However, this is not of practical significance, since this end of the curve represents the tube when empty. The equation of this line is

$$(1-a/A) = 2.62(w/D-1)^{1.88}. \quad (19)$$

The term $(w/D-1)^{1.88}$ was expanded by the binomial theorem in which

$$(a \pm b)^n = (w/D-1)^{1.88}. \quad (20)$$

This expression when expanded and substituted into equation 19 yielded

$$\begin{aligned} a/A &= 1 - 2.62(w/D)^{1.88} + 5.06(w/D)^{0.88} - 2.35(w/D)^{-0.88} \\ &\quad - 0.055(w/D)^{-1.88} - 0.015(w/D)^{-2.88} - 0.0061(w/D)^{-3.88} - \dots \end{aligned} \quad (21)$$

The scatter of points at the lower end of the curves shown in figures 6 and 7 is exaggerated by the expanded scale of the logarithmic

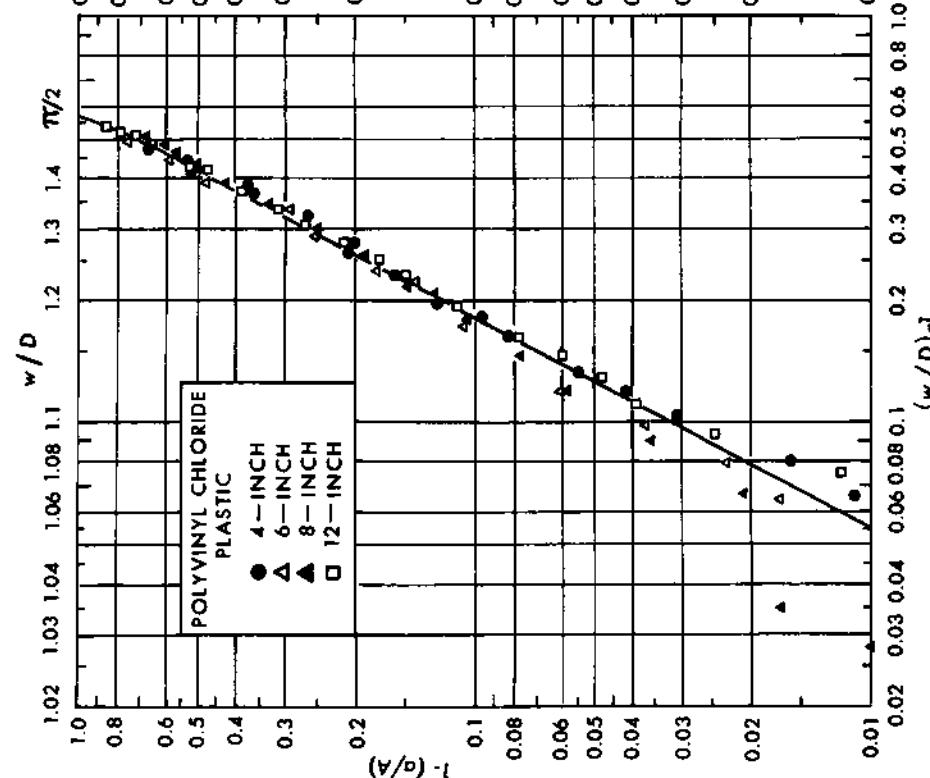


FIGURE 7.—Relation of tube width to the area on logarithmic plot for lay-flat polyvinyl chloride plastic tubing.

and-smaller butyl tubes was less than that of the vinyl tubes for a given hydrostatic head or tube height.

This area reduction was caused by a fold or crease that formed at the two edges of the butyl rubber tubing when it was packaged and stored in a lay-flat position. Since the material was relatively stiff, the creases were semipermanent and remained until the fluid pressure inside the tube was sufficient to straighten them out. The area, particularly at low heads, was therefore reduced. When the tube approached a full-round shape, the head was sufficient to cause the creases to disappear and the cross-sectional area then approached that of a polyvinyl chloride plastic tube. The difference was more pronounced in tubes of small diameter than with those of a large diameter and also with new tubes as compared with those that had been in use for a time. With continued use, the creases would become less pronounced or disappear. The area ratio of the butyl rubber tubes would then approach the same value as that for the thin-walled tubes when related to the tube height and the hydrostatic head.

The results showed that the cross-sectional area when related to tube width varied with the type of tubing and also with the diameter of the butyl tubing. Figure 8 shows data from the thick-walled butyl tubing superimposed upon the area-tube width curve for the vinyl tubing that was shown in figure 5. The area ratio for the very flexible thin-walled vinyl chloride tubes having the same wall thickness was represented by a single curve. A separate curve was required to represent the area ratio of each of the butyl rubber tubes tested. These differences in the area, when related to the tube width, were apparently caused by the difference in tubing wall stiffness and also by the edge creases. As these effects decrease, it would be expected that all tubing of like material could be represented by the same curve and that the curves would approach more nearly that of a completely flexible tube.

For the tubes tested, the test results indicate that the data, when expressed in dimensionless ratios, may be represented by the same curves, whether or not the data are expressed in ratios representing inside or outside dimensions. However, for α to represent the inside area of the tube cross section, the parameters d/D , w/D , and A , used in its determination, must also represent inside dimensions. This is particularly true of such thick-walled tubes as the butyl rubber tubes tested.

Alternative Method to Determine Tube Area

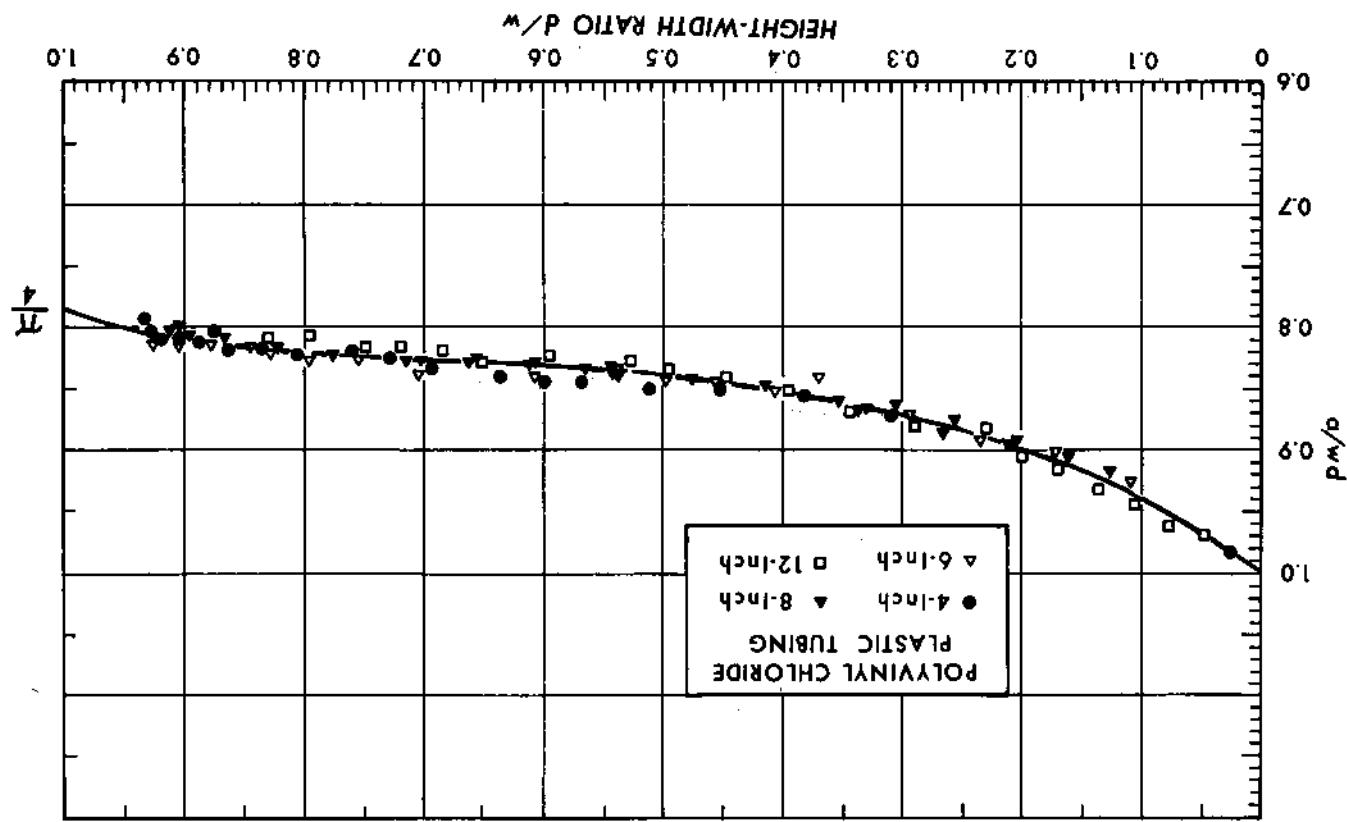
The cross-sectional area of a tube may be determined from the product of the tubing's height-width dimensions multiplied by some factor. As the tube becomes circular, the height and width dimensions each approach the diameter and the factor approaches $\pi/4$. With little or no hydrostatic head, the tube cross section approaches that of a rectangle for which the factor approaches a value of unity. Quantitatively, this factor is a dimensionless number representing the ratio a/wd and is shown plotted versus tube shape, as represented by the height-width ratio (fig. 9). This curve was determined from the polyvinyl chloride plastic tube tests and will not apply to butyl

coordinate paper in this region. The binomial expansions of the foregoing relationships are more complex than those given by equations 14 and 19 before being expanded. The expansions, therefore, offer no particular advantage, but are of academic interest only. The most practical form for the presentation and use of these data is by the use of curves, such as that shown in figure 4.

Butyl Rubber Tubes

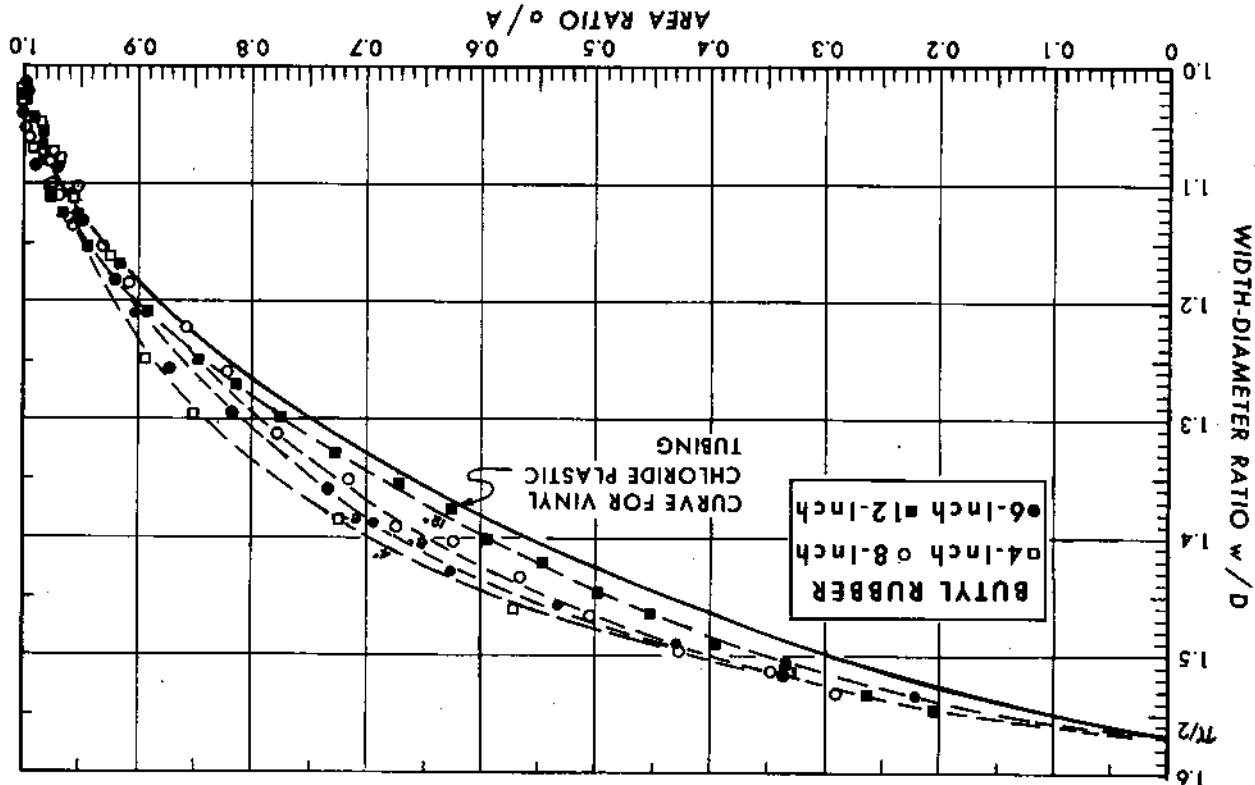
Data from the thick-walled butyl rubber tubes were compared with corresponding data from the polyvinyl chloride plastic tubes. For the tubing tested, the same curves may, in general, be used to describe the area of both polyvinyl chloride plastic and 8-inch-or-larger butyl rubber tubes when related to the hydrostatic head or tube-height parameters. The results indicate, however, that the area of 6-inch-

FIGURE 9.—The ratio a/w_d related to the height-width ratio for lay-flat polyvinyl chloride plastic tubing.



Vinyl chloride plastic tubing.

FIGURE 8.—Area-tube width relationship of butyl rubber tubing superimposed on the corresponding curve for nylon-supported poly-



rubber tubing unless the side creases in the tubes have disappeared either through use or because of the fluid pressure in the tube.

Effect of Fluid Density Upon Tube Shape

Corresponding data from tests conducted with fluids of different specific weights were also represented by the curves shown in figures 4, 5, and 9 when the hydrostatic head was expressed as a column height of the respective fluid. When the pressure head of the different fluids was expressed as the height of a column of water, however, there was a difference in the head-area relation, as shown in figure 10. In contrast to head-area curves, the individual curves representing the oil and brine fluids, in effect, are pressure-area curves for a particular fluid but generalized as to tube size. The three curves of figure 10 indicate that the greater the fluid density, the greater the pressure required to yield a given cross-sectional area.

The pressure head parameter H/D is an abbreviated form of the parameter $\frac{P}{\gamma D}$. When the tube area, represented by a/A , is plotted

against $\frac{P}{\gamma D}$, the resulting curve is a generalized pressure-area curve for fluids of different density. When the parameter H/D is used in place of $\frac{P}{\gamma D}$, it is implied that H represents the hydrostatic head of the respective fluid. When it does, the H/D vs. a/A curve (solid line curve of fig. 10) is a generalized curve for different fluids. This is not true of the broken line curves of figure 10, since H for them does not represent their respective fluid but is expressed as a column height of water. The variation in density of waters used for irrigation is relatively small. Therefore, when lay-flat tubing is used for irrigation, the effect of fluid density upon tube shape is so small that it becomes a matter of interest only and is not of practical significance.

DISCUSSION OF RESULTS

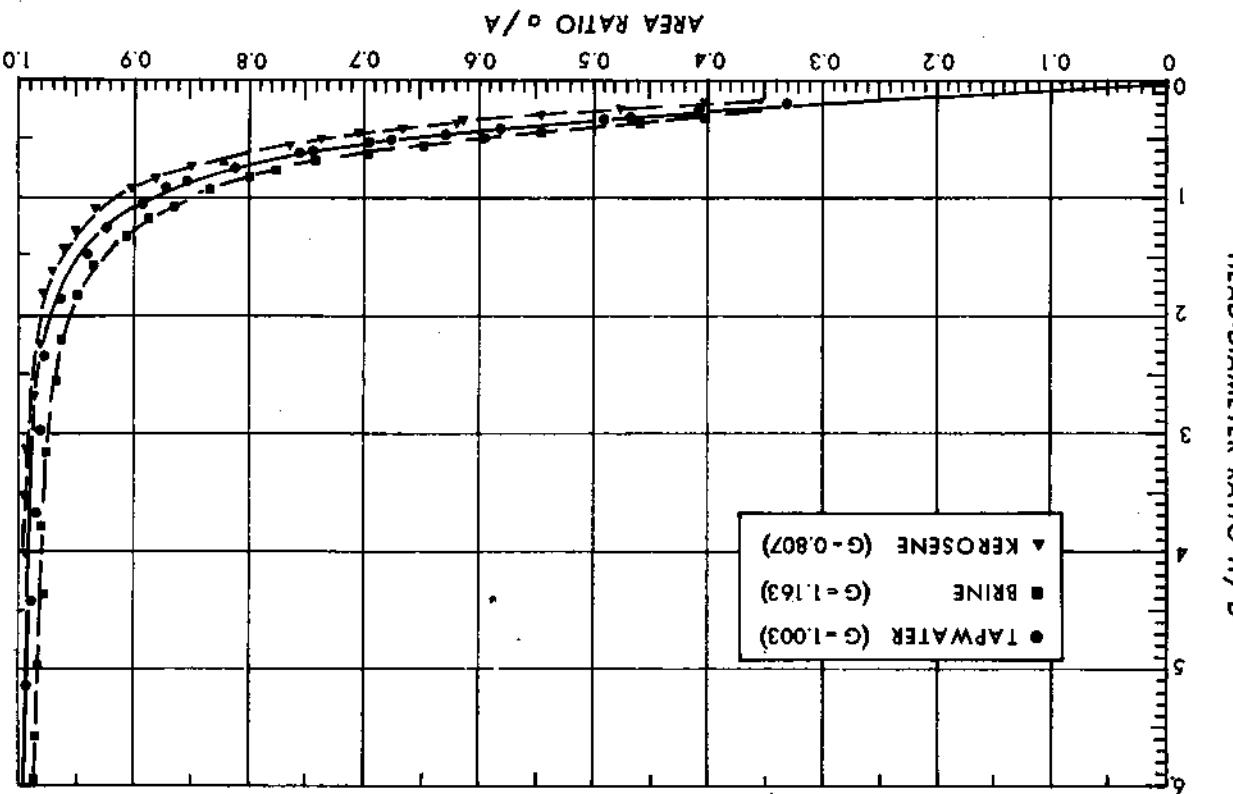
From the data that have been presented, it is possible to determine the cross-sectional area and describe the tube shape, as represented by the height-width ratio, for lay-flat tubing of any degree of roundness. To do this, the full-round diameter must be known and any one of the following: tube height, tube width, or both, or the hydrostatic head. With the area ratio and the full-round area known, the tube cross-sectional area may be readily obtained.

With the area known, the mean flow velocity and the hydraulic radius are easily determined. The hydraulic radius may be obtained directly from the area ratio, since

$$\frac{a}{A} = \frac{r}{R}$$

where r/R is the ratio of the hydraulic radius for a tube at any shape to the hydraulic radius of a full-round pipe. Tube width, because of the influence of tubing wall thickness and stiffness, is not the best

Figure 10.—The area of lay-flat polyvinyl chloride plastic tubing filled with fluids of different specific weights related to the head in which the pressure head of the fluid is expressed as the height of a column of water.



single parameter to use in determining the tube area. The H/D vs. a/A curve (fig. 10) becomes very steep when the tubing approaches a circular shape. Therefore, special care must be exercised when the tube area is determined from this region of the curve.

The tube height is a good parameter from which to determine the area ratio throughout the entire shape range. For most applications, the curve in figure 4 showing the relation of hydrostatic head, tube height, area, and height-width ratio will find the most frequent use. Since these data were obtained with the tubing supported by a flat surface level in a direction perpendicular to the tube length, they are most applicable to tubes supported in this manner. This represents an ideal condition; further research will be needed to determine the deviation therefrom when a tube is supported by a rough or side sloping surface.

The cross-sectional area of tubing, 4 to 16 inches inside diameter, was computed for different degrees of tubing roundness and at different head-diameter and height-diameter ratios (table 2). These values are applicable to all types of lay-flat tubing when supported on a relatively flat surface except thick-walled tubing, such as butyl rubber approximately 6 inches and smaller in diameter. The cross-sectional area of this tubing may be slightly less than that indicated in the table.

FLOW TESTS

The flow-testing phase of this study was undertaken to determine the effect of tubing shape upon the friction coefficient and to obtain data from which the shape factor in equation 12 could be evaluated.

EXPERIMENTAL PROCEDURE

Flow tests were conducted with 6- and 8-inch nylon-supported polyvinyl chloride plastic experimental tubing. An 80-foot, slope adjustable ramp was used to support the tubes on which the flow tests were made (fig. 11). The tubing at the intake end was fastened to a 12-inch water supply line. Water from the tube discharged freely into an open flume at the lower end of the ramp. Flow rates of 1 c.f.s. and greater were measured with a 12-inch flowmeter installed in the supply line, whereas lesser flow rates were determined with a small weighing tank.

Coreless valve stems were secured to the bottom of the tube at 5-foot intervals along the test section. Clear plastic tubing connected the valve stems to a manometer board from which the piezometric pressure head at each 5-foot station was measured (fig. 12). Geometrical dimensions of the tube were measured during the tests. The tube height was measured with a point gage mounted on a stand that straddled the tube (fig. 13). The stand was also fitted with a scale with which to measure the horizontal width of the tubing. The perimeter varied slightly along the tube and, therefore, was measured with a small metallic rule at each station.

Tests were made on each tube, with the tube resting on a 0-, $\frac{1}{2}$ -, 1-, and 2-percent slope. Runs were also made at zero slope with a 6-inch tube full round.

TABLE 2.—Cross-section area of lay-flat tubing of different diameters at different degrees of roundness

Cross-section area for tube size (inside diameter, inches)									
Height-width ratio (a/A) ¹	Area ratio (a/A) ¹	Head-diameter ratio (H/D)	Height-diameter ratio (a/D)	4	6	8	10	12	14
1.000	1.000	1.000	0.5454	0.7864	1.069	1.068	1.065	1.063	1.061
0.975	0.999	1.090	0.873	0.985	0.963	0.9491	0.9373	0.925	0.913
0.950	0.998	1.090	0.872	0.985	0.963	0.9487	0.9362	0.924	0.912
0.925	0.996	1.090	0.871	0.985	0.963	0.9484	0.9360	0.9247	0.913
0.900	0.994	1.090	0.870	0.985	0.963	0.9483	0.9356	0.9242	0.912
0.875	0.986	1.090	0.869	0.985	0.963	0.9482	0.9355	0.9241	0.911
0.850	0.980	1.090	0.868	0.985	0.963	0.9481	0.9354	0.9240	0.909
0.825	0.976	1.090	0.867	0.985	0.963	0.9480	0.9353	0.9239	0.898
0.800	0.970	1.090	0.866	0.985	0.963	0.9479	0.9352	0.9238	0.886
0.775	0.962	1.090	0.865	0.985	0.963	0.9478	0.9351	0.9237	0.875
0.750	0.956	1.090	0.864	0.985	0.963	0.9477	0.9350	0.9236	0.865
0.725	0.942	1.090	0.863	0.985	0.963	0.9476	0.9349	0.9235	0.855
0.700	0.936	1.090	0.862	0.985	0.963	0.9475	0.9348	0.9234	0.845
0.675	0.921	1.090	0.861	0.985	0.963	0.9474	0.9347	0.9233	0.835
0.650	0.906	1.090	0.860	0.985	0.963	0.9473	0.9346	0.9232	0.825
0.625	0.895	1.090	0.859	0.985	0.963	0.9472	0.9345	0.9231	0.815
0.600	0.886	1.090	0.858	0.985	0.963	0.9471	0.9344	0.9230	0.805
0.575	0.874	1.090	0.857	0.985	0.963	0.9470	0.9343	0.9229	0.795
0.550	0.862	1.090	0.856	0.985	0.963	0.9469	0.9342	0.9228	0.785
0.525	0.842	1.090	0.855	0.985	0.963	0.9468	0.9341	0.9227	0.775
0.500	0.821	1.090	0.854	0.985	0.963	0.9467	0.9340	0.9226	0.765
0.475	0.795	1.090	0.853	0.985	0.963	0.9466	0.9339	0.9225	0.755
0.450	0.767	1.090	0.852	0.985	0.963	0.9465	0.9338	0.9224	0.745
0.425	0.742	1.090	0.851	0.985	0.963	0.9464	0.9337	0.9223	0.735
0.400	0.717	1.090	0.850	0.985	0.963	0.9463	0.9336	0.9222	0.725
0.375	0.692	1.090	0.849	0.985	0.963	0.9462	0.9335	0.9221	0.715
0.350	0.667	1.090	0.848	0.985	0.963	0.9461	0.9334	0.9220	0.705
0.325	0.642	1.090	0.847	0.985	0.963	0.9460	0.9333	0.9219	0.695
0.300	0.617	1.090	0.846	0.985	0.963	0.9459	0.9332	0.9218	0.685
0.275	0.592	1.090	0.845	0.985	0.963	0.9458	0.9331	0.9217	0.675
0.250	0.567	1.090	0.844	0.985	0.963	0.9457	0.9330	0.9216	0.665
0.225	0.542	1.090	0.843	0.985	0.963	0.9456	0.9329	0.9215	0.655
0.200	0.517	1.090	0.842	0.985	0.963	0.9455	0.9328	0.9214	0.645
0.175	0.492	1.090	0.841	0.985	0.963	0.9454	0.9327	0.9213	0.635
0.150	0.467	1.090	0.840	0.985	0.963	0.9453	0.9326	0.9212	0.625
0.125	0.442	1.090	0.839	0.985	0.963	0.9452	0.9325	0.9211	0.615
0.100	0.417	1.090	0.838	0.985	0.963	0.9451	0.9324	0.9210	0.605
0.075	0.392	1.090	0.837	0.985	0.963	0.9450	0.9323	0.9209	0.595
0.050	0.367	1.090	0.836	0.985	0.963	0.9449	0.9322	0.9208	0.585
0.025	0.342	1.090	0.835	0.985	0.963	0.9448	0.9321	0.9207	0.575
0.000	0.317	1.090	0.834	0.985	0.963	0.9447	0.9320	0.9206	0.565

16

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Nonuniform Flow

For nonuniform flow, equation 10 was modified to include the accelerative force that accompanies nonuniform flow. The forces that act upon a volume of water flowing nonuniformly are shown in figure 14, in which the accelerative force is represented by the equal and opposite inertial force. The forces maintaining flow are the pressure force, $p_1 a_1 - p_2 a_2$, and the component of weight acting in the direction of flow $\gamma S_o La$ minus the accelerative force $\rho V a \Delta V$. The opposing force is the shear force $\tau_o PL$. For equilibrium, these forces must equal zero. Summation in the x direction gives

$$p_1 a_1 + \gamma S_o La - p_2 a_2 - \tau_o PL - \rho V a \Delta V = 0. \quad (23)$$

The boundary shear stress τ_o may be expressed in terms of the quantity $\rho V^2/2$ and the Darcy-Weisbach resistance coefficient f , thus

$$\tau_o = \frac{f}{4} \frac{\rho V^2}{2} = \frac{f}{8} \rho V^2. \quad (24)$$

Therefore, if τ_o is replaced by $\frac{f}{8} \rho V^2$ and p by γh , equation 23 becomes

$$\gamma h_1 a_1 - \gamma h_2 a_2 + \gamma S_o La = \frac{f}{8} \rho V^2 PL + \rho V a \Delta V \quad (25)$$

from which

$$f = \frac{8\gamma(h_1 a_1 - h_2 a_2 + S_o La)}{\rho V^2 PL} - \frac{8AVR}{VL} \quad (26)$$

in which R was substituted for a/P . A sketch of h and the pressure forces that act on the ends of a section of fluid flow is shown in figure 15. The expression for head loss for nonuniform flow from equation 26 is

$$h_f = f \frac{L}{4R} \frac{V^2}{2g} + \frac{V \Delta V}{g}. \quad (27)$$

This equation is valid for short length increments, but if it is used over a long length-increment, an error would be introduced. When the head loss is expressed in this form, it is assumed that

$$p_1 a_1 - p_2 a_2 = \Delta p_a$$

where p is the average pressure intensity acting on the average area a in which

$$a = \frac{a_1 + a_2}{2}$$

See figures 14 and 15. This assumption is not exactly correct where there is a large difference between the area a_1 and a_2 . The friction

$$(22)$$

$$f = \frac{8Rgh_f}{LV^2}$$

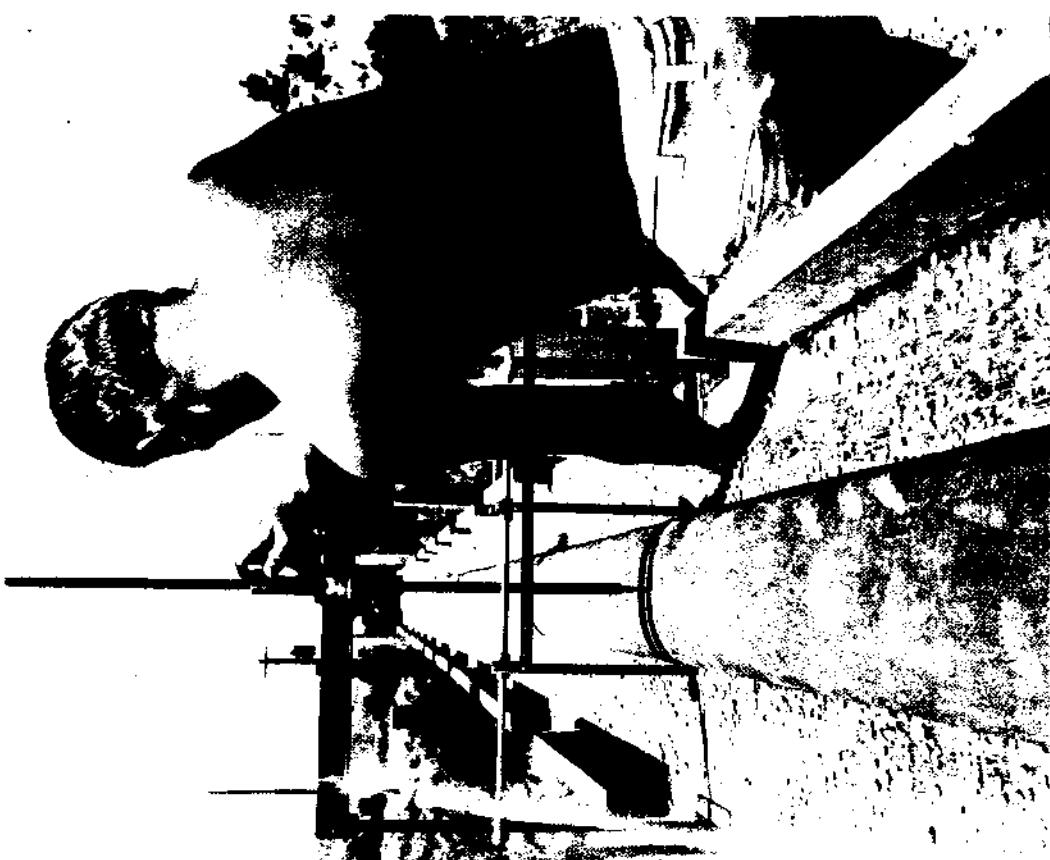


FIGURE 13.—Device used to measure the height and width of polyvinyl chloride plastic tubing during the flow tests. (Gravel was placed on the ramp after the flow tests reported herein were made.)

when the pressure was sufficient to maintain a near-round cross section. In general, however, the flow was nonuniform and the energy grade line was not straight but described an $H-2$, $M-2$, or $M-1$ surface profile curve, depending upon the ramp slope and flow rate. For those runs where uniform flow was approached, the friction coefficient was determined with equation 10 in which

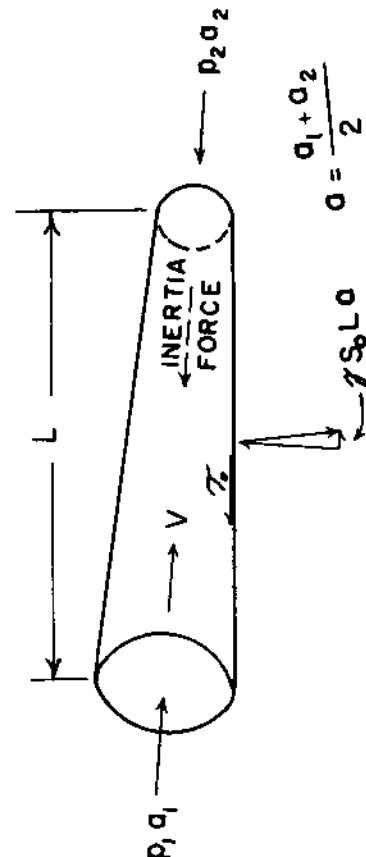


FIGURE 14.—Sketch showing the forces acting on a section of nonuniform fluid flow.

$$a = \frac{a_1 + a_2}{2}$$

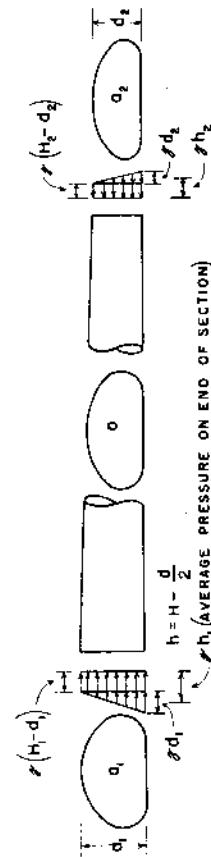


FIGURE 15.—Sketch showing the pressure forces acting on the ends of a flow tube.

coefficient, therefore, for nonuniform flow from the test data was evaluated with equation 26 rather than with equation 27.

The value of f computed from equation 26 generally decreased in value at consecutive stations along the tube toward the lower end. The value from which the shape factors were determined was the average value of f in the first 30 feet of the test section. Because of end effects, the data from stations near the end of the tube were not used to determine f .

Shape Factor

Values of f determined from the experimental data with equations 22 and 26 were used to calculate values of β with equation 11 in which

$$\beta = f/f'$$

Values of f' were obtained from a pipe resistance diagram of friction coefficient versus Reynolds number. Coordinates for this diagram were computed with equations 4, 5, and 6. Values of f' were determined for a pipe of the same diameter and with the same relative roughness as the tubing if the tubing were round. The relative roughness was ϵ/D , where D was the full-round tube diameter, and was constant for each size of tube. Reynolds number for the tubing was conveniently computed from the following relationship:

$$R = \frac{VD}{\nu} = \frac{4RV}{\nu} = \frac{4Q}{\nu Pa} = \frac{4Q}{P_v} \quad (28)$$

The shape factor β is related to the tube shape, represented by the height-width ratio, and is shown by the curve in figure 16. The shape factor represents the effect upon head loss of the change in both velocity distribution and relative roughness caused by shape change. The broken line curves shown in figure 16 indicate the trend of the curve beyond the data. Since a zero value of the ratio d/w represents a parallel boundary conduit of infinite extent, each end point curve was determined by evaluating the shape factor for parallel boundaries. This was accomplished by determining the ratio of the f value for parallel boundary flow to that of pipe flow at a given Reynolds number for different boundary spacings.

A definite end point at $d/w = 0$ for the curve cannot be found, since the f/f' ratio varies with Reynolds number. This variation results from the fact that the family of curves on the resistance diagrams are not parallel to each other from one value of Reynolds number to another. The Colebrook-White transition equation (equation 6) was modified for use with parallel boundary flow. This function, used to define f in the transition region between smooth and rough parallel boundaries, was:

$$\frac{1}{\sqrt{f}} = 2.11 - 2 \log_{10} \left[\frac{k}{r_o} + \frac{19.5}{R \sqrt{f}} \right]. \quad (29)$$

A resistance diagram for parallel boundaries was constructed by plotting values of f , computed with equations 7, 8, and 29, versus Reynolds number for different values of relative roughness. The f values for parallel boundary flow used in the ratio f/f' were taken from this resistance diagram. Also shown in figure 16 is the calculated theoretical shape factor for laminar flow through an elliptical-shaped conduit as given by Lamb.⁹ in which

$$\beta = \frac{2 \beta_{lw}}{(d^2 + w^2)}. \quad (30)$$

This equation is included merely to show a comparison between the shape factor for laminar and turbulent flow through similarly shaped conduits.

With values of the shape factor β known, equation 12 may now be used to represent the frictional head loss for uniform flow through lay-flat tubing.

DISCUSSION

Design Equations for Friction Loss

The head loss for uniform flow through a tube may also be determined in terms of the loss for the same flow through a round rigid pipe of the same size and relative roughness. Since

$$\frac{V^2}{4R} = \frac{\left[\left(\frac{A}{a} \right) V_p \right]^2}{\left(\frac{a}{A} \right) D} = \left(\frac{A}{a} \right)^3 \frac{V_p^2}{D},$$

⁹ LAMB, HORACE. HYDRODYNAMICS. Ed. 6, 587 pp., illus. New York. 1932.

equation 10 may be expressed in the following form:

$$h_f = \left(\frac{A}{a}\right)^3 f' \frac{L}{D} \frac{V_s^2}{2g}. \quad (31)$$

A convenient form, therefore, in which to express equation 12 for the head loss through lay-flat tubing is

$$h_f = \beta \left(\frac{A}{a}\right)^3 f' \frac{L}{D} \frac{V_s^2}{2g}. \quad (32)$$

The factor $\beta \left(\frac{A}{a}\right)^3$ is constant for any given tube shape and is related to the height-width ratio and the head-diameter ratio by the curve shown in figure 17. The loss for uniform flow through a tube may be determined by multiplying the loss for the same flow through a round pipe by the factor $\beta \left(\frac{A}{a}\right)^3$. Equation 32 will probably be the simplest and most practical form to use in designing and evaluating lay-flat tubing for field application.

If the head loss were to be expressed in the form of equation 1, the equation applicable to lay-flat tubing would be

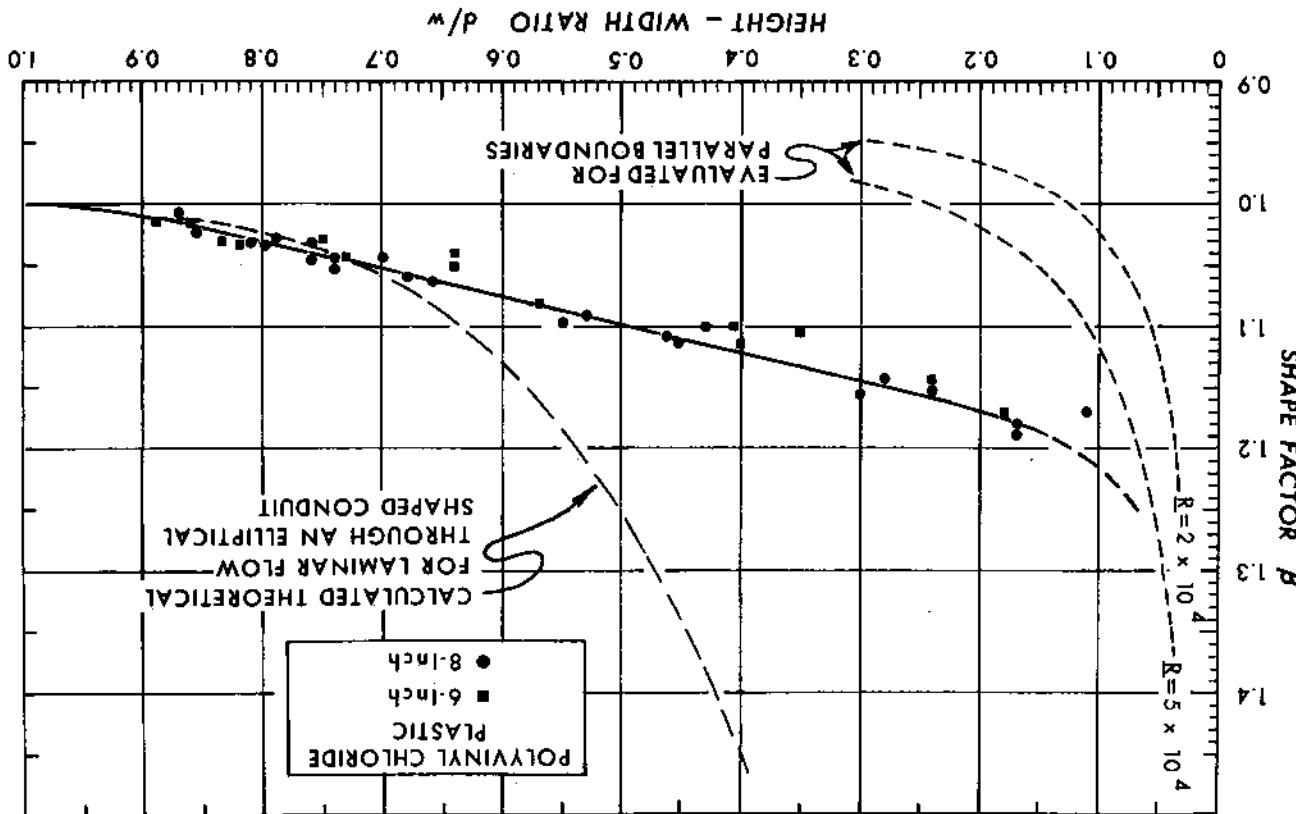
$$h_f = \beta \left(\frac{A}{a}\right)^{3+m} \frac{K L V_s^2}{D^m} \quad (33)$$

in which values of K , V_s , and D are those applicable to the same flow through a pipe of the same size and roughness as the tube when round. Use of the friction coefficient f' may in some cases introduce a small error, since it is determined from the Colebrook-White transition curve on the pipe resistance diagram. This curve is for flow through a pipe of commercial or nonuniform roughness. For tubing that is not hydraulically smooth, the absolute roughness of the material from which it is fabricated will, in most cases, be more uniform than that of commercial pipe. Because of this, the f -Reynolds number relationship may depart slightly from the transition curve toward the curve pattern obtained by Nikuradse¹⁰ in his experiments on pipe of uniform roughness. In most cases the error will likely be very small.

Relative Roughness

As noted previously (p. 2), the tubing relative roughness is affected by a shape change and is difficult to define. For a tube shape intermediate between the two limits of pipe and parallel boundaries, the depth of flow midway between boundaries is different in the width direction from that in the height direction. The problem, therefore, is to represent the two flow depths by a single dimension that will be valid from one shape limit to the other. Four times the hydraulic radius

FIGURE 16.—The shape factor β related to the height-width ratio for lay-flat polyvinyl chloride plastic tubing.



¹⁰ See footnote 5.

is often used to represent this characteristic length. This is valid for open channel flow, but for closed conduits, use of the hydraulic radius introduces an error of two as the cross section approaches the parallel-boundary shape limit. At this limit, the actual relative roughness is two times as great as that indicated when four times the hydraulic radius is used in its determination. The relative roughness for a circular shape is represented by

$$\epsilon/D = \epsilon/4R,$$

whereas for parallel boundaries it is represented by

$$\epsilon/B = \epsilon/2R.$$

In the absence of more precise information, the tube height d would likely be the best parameter from which to compute the actual tubing relative roughness. Use of this dimension would give the correct value when the tube is full round and also as it approaches a rectangular shape, even though it may not be exactly correct at shapes in-between these two limits.

The effect of relative roughness, as related to tube shape, upon the friction coefficient is not separately evaluated in this bulletin but is included in the shape factor β . The hydraulic design is thereby made easier because the roughness value used in determining f' is constant for each tube irrespective of tube shape. If the effect of relative roughness upon head loss were to be represented by the friction coefficient f' instead of β , f' would be determined from a resistance diagram in which the tubing relative roughness would be computed from a representative tube dimension such as tube height. In this case a different shape factor would be required, since the relative roughness effect would be included in f' rather than in the shape factor.

Further Study Needed

The effect of ground surface roughness upon flow through lay-flat tubing may exceed the shape effects. This problem has not yet been studied. The initial laboratory investigation reported herein needs to be supplemented by further study in the field.

The nonuniform flow phase of the problem and the effects of accelerated flow near the end of the tube need further study. Additional information is needed to determine more fully the requirements and performance characteristics of lay-flat tubing materials. Further development of tubing outlets and couplings with their hydraulic characteristics is needed.

DISCHARGE DIAGRAMS

M/P OUTLET HEIGHT-HEAD

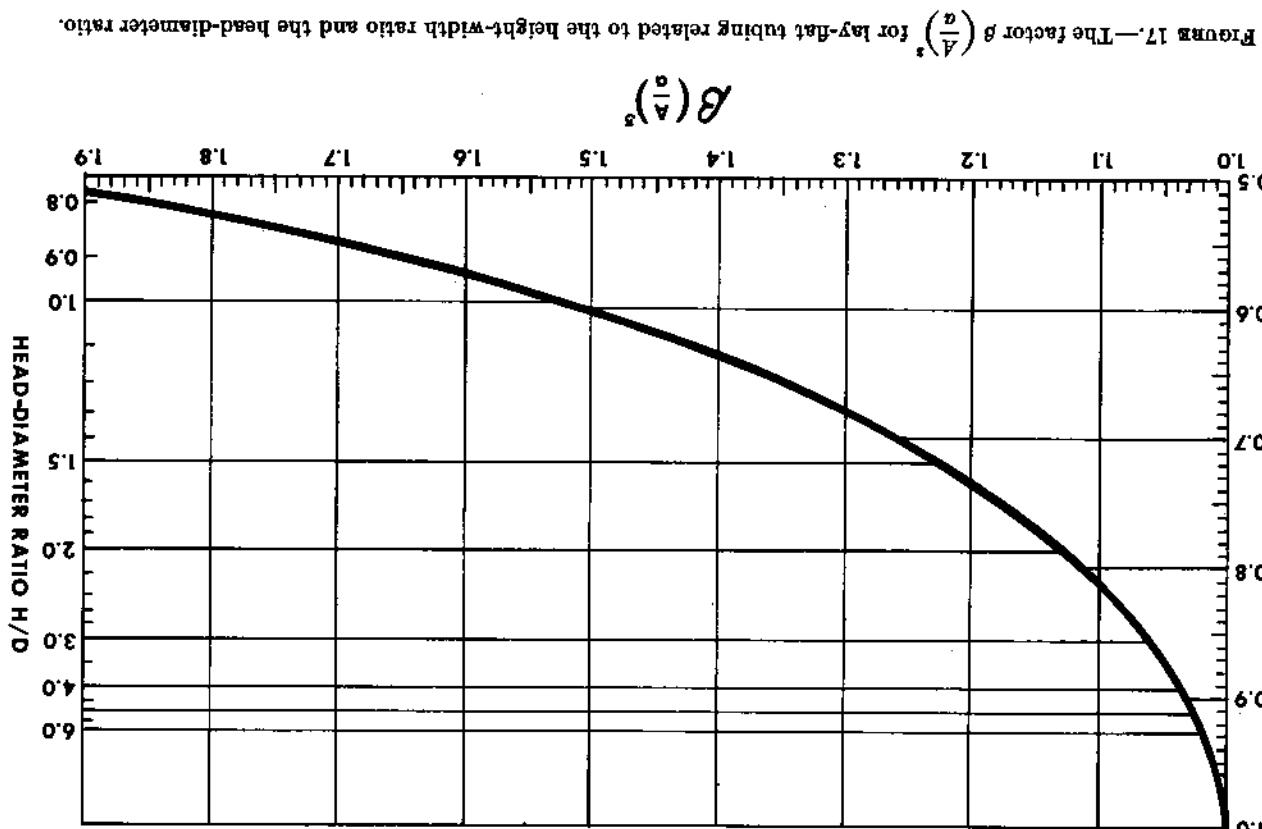


FIGURE 17

FIGURE 17.—The factor $\beta \left(\frac{a}{A} \right)^2$ for lay-flat tubing related to the height-width ratio and the head-diameter ratio.

Typical diagrams relating the discharge to the head loss for irrigation tubing of different diameters and degrees of roundness are shown in figures 18 to 22. These diagrams show the influence of tube shape

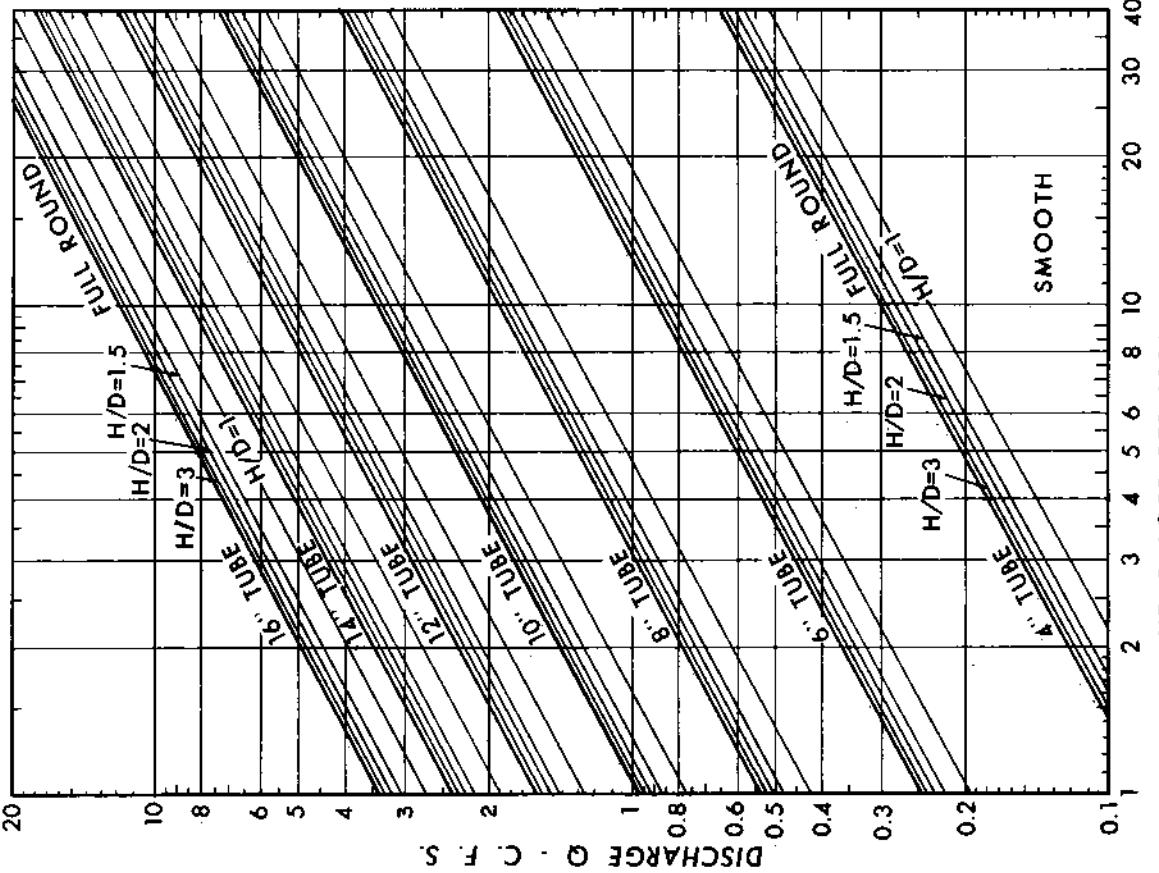


FIGURE 18.—Head-discharge diagram for lay-flat irrigation tubing with smooth boundaries for different degrees of roundness.

upon the discharge for tubes having a boundary varying from smooth to 0.003 inch equivalent roughness. The curves in these figures were computed with equation 32. To use the diagram for tubes at less than a full-round cross section, it is necessary to know the pressure head in the tube. In designing for uniform flow on sloping ground,

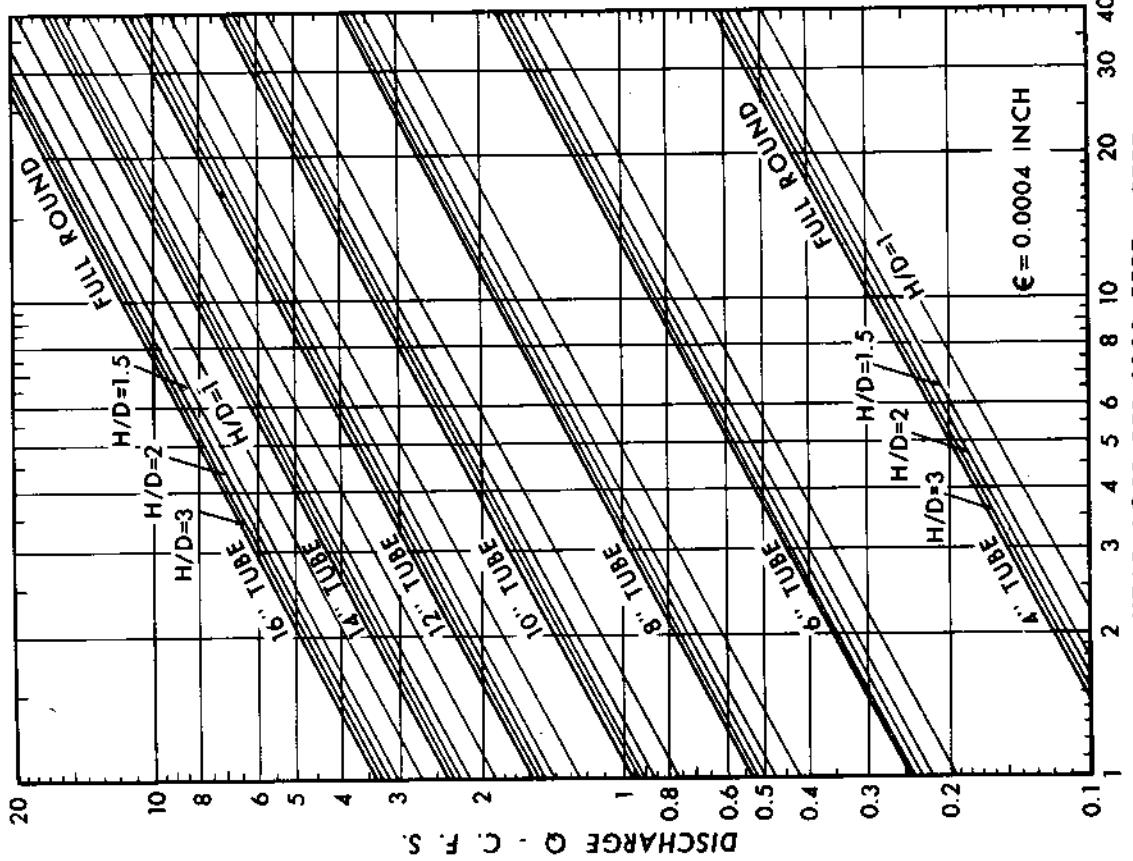


FIGURE 19.—Head-discharge diagram for lay-flat irrigation tubing, $\epsilon = 0.0004$ inch, for different degrees of roundness.

this may be assumed, in most cases, to be the same as the head on the tube at the intake end. The capacity of a tube flowing at less than full-round may be increased by providing for additional head to bring the tube to a more round cross section; a margin of safety may therefore be provided.

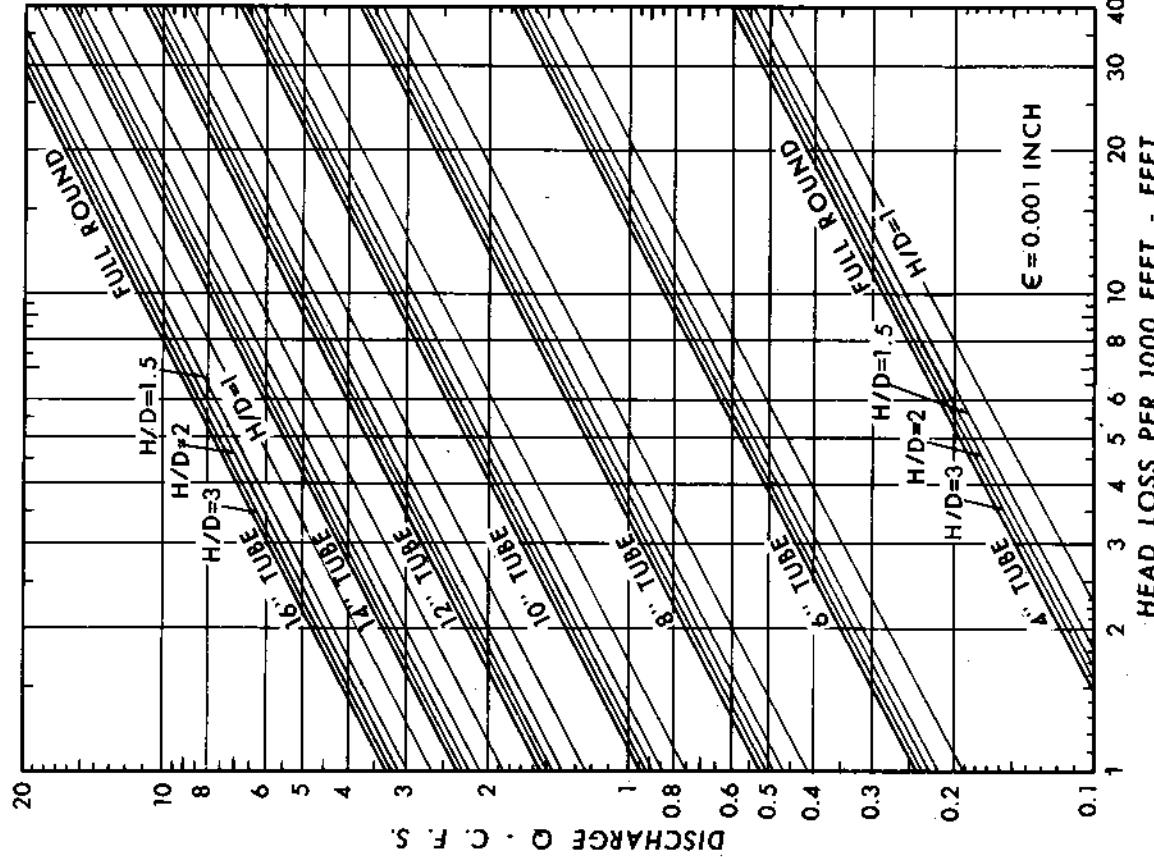


FIGURE 20.—Head-discharge diagram for lay-flat irrigation tubing, $\epsilon = 0.001$ inch, for different degrees of roundness.

Care is needed in using the discharge diagrams for tubing on rough ground surfaces. The friction coefficient does not include the effect of ground surface roughness upon the head loss. Therefore, a margin of safety must be provided by the designer until adequate information is available to evaluate accurately this effect.

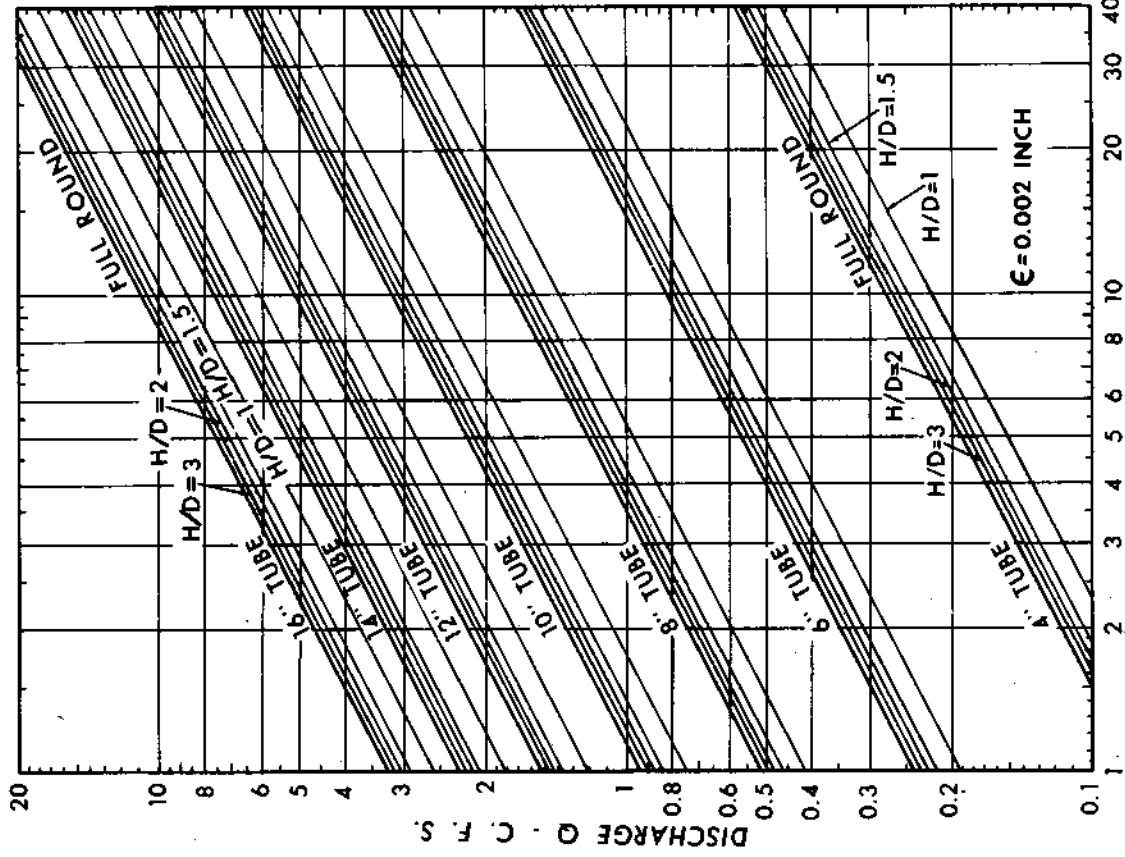


FIGURE 21.—Head-discharge diagram for lay-flat irrigation tubing, $\epsilon = 0.002$ inch, for different degrees of roundness.

Examples are presented to illustrate how figures 18 to 22 may be used in the design of tubing on a smooth ground surface. Minor head losses such as entrance and coupler loss have been omitted to simplify the illustrations.

From figure 22 the head loss would be 4.8 feet per 1,000 feet or a slope of 0.0048.

Problem: If we assume flow is uniform, what size tube will be required to carry 3 c.f.s. at a ground slope of 0.5 percent with a 2-foot head available at the intake. Try a 12-inch tube:

$$H/D = \frac{2A}{12} = 2.0.$$

Head loss per 1,000 feet equals 5 feet. From figure 22 the discharge equals 3.25 c.f.s. A 12-inch tube therefore will be adequate (if tubing boundary roughness is assumed equal to 0.003 inch).

SUMMARY

STATIC TESTS

The hydraulic properties of lay-flat irrigation tubing are closely related to the shape and cross-sectional area of the tube. These characteristics are in turn dependent upon the fluid pressure head inside the tube. A study was undertaken to obtain data from which the pressure-shape-area relations could be determined. The cross section of tubing at various hydrostatic pressure heads was traced with a special pantograph. Tracings were made on supported polyvinyl chloride plastic and butyl rubber tubes of different diameters. The areas of the cross-sectional tracings was measured and related to the hydrostatic head, tube height, width, height-width ratio, and height-width product. The results, expressed in dimensionless ratios, are shown in figures 4 to 10.

The cross-sectional area of tubing 4 to 16 inches in diameter for different degrees of tubing roundness was determined and is presented in table 2.

FLOW TESTS

A study was also undertaken to determine the effect of tube shape upon the frictional head loss. Flow tests were conducted on 6- and 8-inch nylon-supported polyvinyl chloride experimental tubing. Frictional head loss for uniform flow through the tubing was expressed in the form of the Darcy-Weisbach equation in which

$$h_f = f \frac{L}{4R} \frac{V^2}{2g}.$$

Problem: Determine the ground slope required to maintain

uniform flow of 2 c.f.s. flowing through a 10-inch-diameter tube having a roughness of 0.003 inch, with a head of 2 feet provided at the intake.

$$\text{Head-diameter ratio } \frac{H}{D} = \frac{24}{10} = 2.4.$$

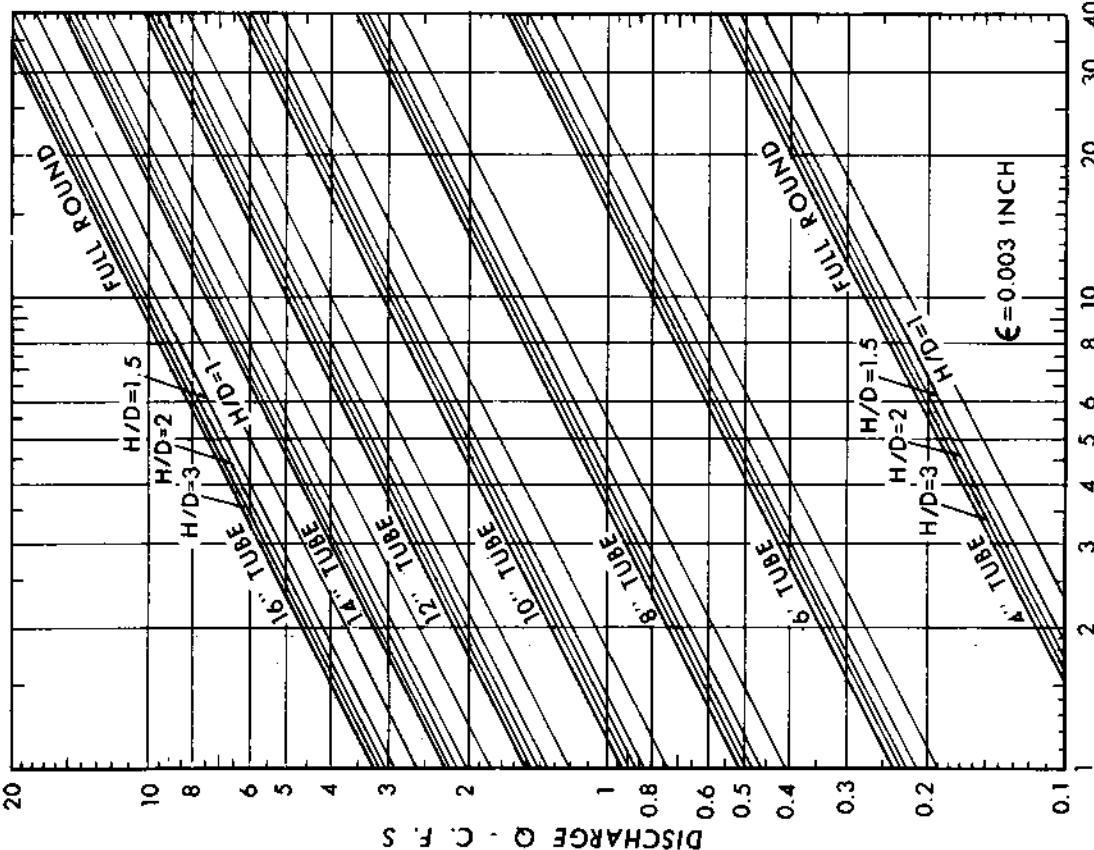


FIGURE 22.—Head-discharge diagram for lay-flat irrigation tubing, $\epsilon = 0.003$ inch, for different degrees of roundness.

Problem: Determine the Darcy-Weisbach equation in which

$$h_f = f \frac{L}{4R} \frac{V^2}{2g} + \frac{V \Delta V}{g}.$$

The friction coefficient f is equal to $\beta f'$ where β is a shape factor that varies with tube shape. The friction coefficient f' is for an equivalent

Symbol	Dimension	Definition
A	L_1	Cross-sectional area of a circular flow conduit and of a flexible tube when fully round.
B	L_2	Cross-sectional area of tube or conduit less than full round.
C	L_3	Diameter of a round boundary spacing.
D	L_4	Diameter of a tube or flow conduit when fully round.
E	L_5	Fractional height of a tube or flow conduit.
F	L_6	Fractional coefficient for a full-round tube or for a rigid pipe of the same diameter and roughness, and at the same Reynolds number and equivalent diameter when compared to a pipe of the same diameter and roughness, and at the same head loss.
G	L_7	Acceleration of gravity = 32.2 ft/sec^2 .
H	L_8	Pressure head of fluid in the tube.
I	L_9	Reynolds number of a tube = $\frac{H}{d} \cdot \frac{D}{d}$.
J	L_{10}	Friction factor for a rigid pipe of a given diameter and roughness.
K	L_{11}	Friction factor for a rigid pipe of a given head loss.
L	L	Hydraulic radius = $\frac{\text{area}}{\text{perimeter}}$.
M	L_2	Head loss due to friction in a tube.
N	L_3	Head loss due to friction in a rigid pipe.
O	L_4	Head loss due to friction in a rigid pipe.
P	L_5	Head loss due to friction in a rigid pipe.
Q	L_6	Head loss due to friction in a rigid pipe.
R	L_7	Head loss due to friction in a rigid pipe.
S	L_8	Head loss due to friction in a rigid pipe.
T	L_9	Head loss due to friction in a rigid pipe.
U	L_{10}	Head loss due to friction in a rigid pipe.
V	L_{11}	Head loss due to friction in a rigid pipe.
W	L_{12}	Head loss due to friction in a rigid pipe.
X	L_{13}	Head loss due to friction in a rigid pipe.
Y	L_{14}	Head loss due to friction in a rigid pipe.
Z	L_{15}	Head loss due to friction in a rigid pipe.
a	A	Area of a rigid pipe.
b	A_1	Area of a rigid pipe.
c	A_2	Area of a rigid pipe.
d	A_3	Area of a rigid pipe.
e	A_4	Area of a rigid pipe.
f	A_5	Area of a rigid pipe.
g	A_6	Area of a rigid pipe.
h	A_7	Area of a rigid pipe.
i	A_8	Area of a rigid pipe.
j	A_9	Area of a rigid pipe.
k	A_{10}	Area of a rigid pipe.
l	A_{11}	Area of a rigid pipe.
m	A_{12}	Area of a rigid pipe.
n	A_{13}	Area of a rigid pipe.
o	A_{14}	Area of a rigid pipe.
p	A_{15}	Area of a rigid pipe.
q	A_{16}	Area of a rigid pipe.
r	A_{17}	Area of a rigid pipe.
s	A_{18}	Area of a rigid pipe.
t	A_{19}	Area of a rigid pipe.
u	A_{20}	Area of a rigid pipe.
v	A_{21}	Area of a rigid pipe.
w	A_{22}	Area of a rigid pipe.
x	A_{23}	Area of a rigid pipe.
y	A_{24}	Area of a rigid pipe.
z	A_{25}	Area of a rigid pipe.

SYMBOLS AND DEFINITIONS

The head loss for uniform flow through tubing, when compared to the same flow through a round pipe of the same size and roughness, determines the discharge for irrigation tubing of different diameters and degrees of roundness to the head loss presented.

Diameters relating the discharge for irrigation tubing of different sizes to the head loss to the head loss of a rigid pipe of a given diameter and roughness, determined from a conventional pipe resistance diagram.

The head loss for uniform flow through tubing, when compared to the same flow through a round pipe of the same size and roughness, determines the discharge for irrigation tubing of different sizes to the head loss to the head loss of a rigid pipe of a given diameter and roughness.

$$\text{varied as the product of } g \left(\frac{A}{d} \right)^n .$$

The head loss for uniform flow through tubing, when compared to the same flow through a round pipe of the same size and roughness, determines the discharge for irrigation tubing of different sizes to the head loss to the head loss of a rigid pipe of a given diameter and roughness.